## ENGINEERING ECONOMY

## Depreciation \& Income Tax

## Definition

"Loss of value for a fixed/current asset"
$\square$ Current assets are balance sheet accounts that represent the value of all assets that can reasonably expect to be converted into cash within one year.
$\square$ Current assets are important to businesses because they can be used to fund day-to-day operations and pay ongoing expenses.

## Why Do We Consider Depreciation?

## Business Expense: Depreciation is viewed as a part of business expenses that reduce taxable income.

## Gross Income -Expenses: <br> (Cost of goods sold) <br> (Depreciation) <br> (operating expenses)

Taxable Income

- Income taxes

Net income (profit)

## Depreciated Assets

* Assets used in business or held for production of income
* Assets having a definite useful life and a life longer than one year (you can never depreciate land)
Assets that must wear out, become obsolete or lose value


## Depreciated Assets

A qualifying asset for depreciation must satisfy all of the three conditions above. Ex: buildings, machinery, equipment, vehicles etc.

The depreciated assets are not valid to inventory or stock sale, or investment property.

## Terms in Depreciation

$\square$ Useful life - how many years will an asset be useful to a company?
$\square$ Salvage value - Asset's estimated value at the end of its useful life. 10\% rule of the initial value
$\square$ Book value BVt - Remaining undepreciated capital investment in year $\dagger$

## Depreciation Method

## Straight of Line Depreciation (SLD)

## Sum of Years Digits Depreciation (SOYD)

Amount of depreciation Amount of depreciation cost is equal annually

Annual Depreciation:
SLD $=\frac{1}{N}(I-S)$ cost isn't equal annually

- Based on sum of years digit
Annual depreciation:
$\mathrm{SOYD}_{\mathrm{t}}=\frac{N-(\mathbf{t}-\mathbf{1})}{\Sigma \text { digit }}(I-S)$
$\mathrm{N}=$ useful life
(recovery period)
I = investment
$S=$ salvage value
$\sum$ digit $=\frac{N}{2}(N+1)$
$\mathrm{N}=$ useful life (recovery period)
$t=\operatorname{period}($ year $t)$


## Double Declining Balance Depreciation (DDBD)

- Amount of depreciation cost isn't equal annually

$$
\operatorname{DDBD}_{\mathrm{n}}=\frac{2 \mathrm{I}}{\mathrm{~N}}\left(1-\frac{2}{\mathrm{~N}}\right)^{\mathrm{n}-1}
$$

$$
\mathrm{BV}_{\mathrm{n}}=\mathrm{I}\left(1-\frac{2}{\mathrm{~N}}\right)^{\mathrm{n}}
$$

$N=$ useful life (recovery period)
| = investment

## Straight of Line Depreciation (SLD)

$\square$ Travel agent has mini bus Rp 150 million. The useful life of the minis bus is 5 years and it can be sold $\operatorname{Rp} 50$ million at the end of its life.
$\square$ Estimate the annual depreciation
$\square$ Total of 3 years depreciation
$\square$ Book value after three years usage using SLD method

## Answer

Annual depreciation:
SLD $=\frac{1}{N}(I-S)$
SLD $=\frac{1}{5}(150-50)$
SLD = Rp 20 million/years

## Apply to the table


$\square$ Total of depreciation cost after 3 years usage:

- $\operatorname{Dep}_{\mathrm{t}}=\frac{t}{N}(I-S)$
$\sum$ Dep $_{3}=\frac{3}{5}(150-50)$
$\Sigma \operatorname{Dep}_{3}=\operatorname{Rp} 60$ Million
$\square$ Book value at the end of year 3:
$B V_{3}=1-\sum D^{2} p_{3}$
$B V_{3}=150-60$
$B V_{3}=90$ juta


## Sum of Years Digits Depreciation (SOYD)

Travel agent has mini bus Rp 150 million. The useful life of the minis bus is 5 years and it can be sold $\operatorname{Rp} 30$ million at the end of its life.
$\square$ Remarks :
Investment(I) = Rp 150 milion salvage value(S)=Rp 30 milion useful life $(N)=5$ years

## The first step for SOYD method

Calculate the value of digit!
$\sum$ digit $=\frac{N}{2}(N+1)$

- digit $=\frac{5}{2}(5+1)$
$\square$ digit $=15$


## Calculate annual depreciation

$$
\begin{aligned}
& \text { SOYD }_{\mathrm{t}}=\frac{N-(t-1)}{\Gamma \text { digit }}(I-S) \\
& \mathrm{t}=1 \rightarrow \text { SOYD }_{\mathrm{t}}=\frac{5-(\mathbf{1 - 1 )}}{15}(\mathbf{1 5 0}-\mathbf{3 0})=\frac{5}{15}(\mathbf{1 2 0})=40 \\
& \mathrm{t}=2 \rightarrow \text { SOYD }_{\mathrm{t}}=\frac{5-(2-1)}{15}(\mathbf{1 5 0}-\mathbf{3 0})=\frac{4}{15}(\mathbf{1 2 0})=32 \\
& \mathrm{t}=3 \rightarrow \text { SOYD }_{\mathrm{t}}=\frac{3-(\mathrm{s-1})}{15}(\mathbf{1 5 0} \mathbf{- 3 0})=\frac{3}{15}(\mathbf{1 2 0})=\mathbf{2 4} \\
& \mathrm{t}=4 \rightarrow \text { SOYD }_{\mathrm{t}}=\frac{5-(4-1)}{15}(\mathbf{1 5 0}-\mathbf{3 0})=\frac{2}{15}(\mathbf{1 2 0})=16 \\
& \mathrm{t}=5 \rightarrow \mathrm{SOYD}_{\mathrm{t}}=\frac{\mathbf{5 - ( 5 - 1 )}}{15}(\mathbf{1 5 0}-\mathbf{3 0})=\frac{1}{15}(\mathbf{1 2 0})=8
\end{aligned}
$$

## Apply to the table

| N | BV | SOYD | $\sum$ Dep |
| :---: | :---: | :---: | :---: |
| 0 | 150 |  |  |
| 1 | 110 | 40 | 40 |
| 2 | 78 | -32 | 72 |
| 3 | 54 | 24 | 96 |
| 4 |  | 16 | 112 |
| 5 | 30 | 8 | 120 |

book value $=$ salvage then $\rightarrow$ STOP !

## Now if we use DDBD method

$\square$ Remarks :
Investment(I) = Rp 150 milion salvage value $(S)=R p 30$ milion useful life $(N)=5$ years
$\operatorname{DDBD}_{\mathrm{n}}=\frac{2 \mathrm{I}}{\mathrm{N}}\left(1-\frac{2}{\mathrm{~N}}\right)^{\mathrm{n}-1}$
$\mathrm{DDBD}_{1}=\frac{2(150)}{5}\left(1-\frac{2}{5}\right)^{1-1}=60$
$\mathrm{DDBD}_{2}=\frac{2(150)}{5}\left(1-\frac{2}{5}\right)^{2-1}=36$
$\mathrm{DDBD}_{4}=\frac{2(150)}{5}\left(1-\frac{2}{5}\right)^{4-1}=12,96$
$\mathrm{DDBD}_{5}=\frac{2(150)}{5}\left(1-\frac{2}{5}\right)^{5-1}=7,776$
$\mathrm{DDBD}_{3}=\frac{2(150)}{5}\left(1-\frac{2}{5}\right)^{3-1}=21,6$

$$
\mathrm{BV}_{5}=150\left(1-\frac{2}{5}\right)^{5}=11,66
$$

## Apply to the table

| $N$ | BV | DDBD | ミDep |
| :---: | :---: | :---: | :---: |
| 0 | 150 | $(-)$ |  |
| 1 | 90 | $(=)$ | 60 |
| 2 | 54 | 36 | 60 |
| 3 | 32,4 | 21,6 | 96 |
| 4 | 19,44 | 12,96 | 130,56 |
| 5 | 11,66 | 7,78 | 138,34 |

book value $\neq$ salvage value

## Book Value Problem

$\square$ DDBD $\rightarrow$ if we using this method
" book value $\neq$ salvage value"
$\square$ If Book value ${ }_{t=n}>$ salvage value $\rightarrow$ problem If Book value ${ }_{t=n}=$ salvage value then OK If Book value $\mathrm{t}_{\mathrm{t}}$ < salvage value then OK

Some nations permits zero residual value (the smallest value)

## Book Value Problem

Book value $_{t=n}>$ salvage value "it will be sunk cost and must be avoided"

How to solve this problem $\rightarrow$

1. Continue the calculation of depreciation using 2 methods DDBD and SLD
2. However you have to change SLD formula into this:

$$
S L D_{t}=\frac{1}{N-(n-1)}\left(\mathrm{BV}_{\mathrm{t}-1}-\mathrm{S}\right)
$$

## Book Value Problem

$$
S L D_{t}=\frac{1}{N-(n-1)}\left(B V_{t-1}-S\right)
$$

$\square \mathrm{N}-(\mathrm{n}-1)=$ remaining recovery period
$\square \mathrm{BV}_{\mathrm{t}-1} \quad=$ book value from previous year using DDBD method

## Book Value Problem

1. Continue the calculation of depreciation using 2 methods DDBD and SLD
2. Select larger depreciation amount
3. When SLD $\geq$ DDBD, the switching is conducted

## Practice Problem

$\square$ Travel agent has purchased second bus worth to Rp 700 million. The useful life of the bus is 5 years and it can be sold Rp 30 million at the end of its life.
$\square$ Remarks :
Investment(I) $=\operatorname{Rp} 700$ milion
salvage value $(S)=\operatorname{Rp} 30$ milion
useful life $(N)=5$ years

## Answer

Investigate the book value at the end of period

$$
\begin{aligned}
& \mathrm{BV}_{\mathrm{n}}=\mathrm{I}\left(1-\frac{2}{\mathrm{~N}}\right)^{\mathrm{n}} \\
& \mathrm{BV}_{5}=700\left(1-\frac{2}{5}\right)^{5}=54,432
\end{aligned}
$$

Book value > salvage value- $\rightarrow$ DDBD to SLD

## One by one step DDBD to SLD



## DDBD to SLD conversion

| t | $\mathbf{S L D}_{\mathbf{t}}=\frac{1}{N-(n-1)}\left(\mathbf{B V}_{\mathrm{t}-1}-\mathbf{S}\right)$ | $\operatorname{DDBD}_{\mathrm{n}}=\frac{2 I}{N}\left(1-\frac{2}{N}\right)^{\mathrm{n}-1}$ | $\mathbf{B V} \mathbf{n}_{\mathbf{n}}=I\left(1-\frac{2}{N}\right)^{\mathrm{n}}$ | Remarks |
| :---: | :---: | :---: | :---: | :---: |
| 0 |  | ------------- | 700 |  |
| 1 | $\frac{1}{5-(1-1)}(700-30)=134$ | $\frac{2(700)}{5}\left(1-\frac{2}{5}\right)^{1-1}=280$ | $700-280=420$ | DDBD |
| 2 | $\frac{1}{5-(2-1)}(420-30)=97.5$ | $\frac{2(700)}{5}\left(1-\frac{2}{5}\right)^{2-1}=168$ | $420-168=252$ | DDBD |
| 3 | $\frac{1}{5-(3-1)}(252-30)=74$ | $\frac{2(700)}{5}\left(1-\frac{2}{5}\right)^{3-1}=100.8$ | 252-100.8=151.2 | DDBD |
| 4 | $\frac{1}{5-(4-1)}(151.2-30)=60.6$ | $\frac{2(700)}{5}\left(1-\frac{2}{5}\right)^{4-1}=60.48$ | 151.2-60.6=90.6 | Switch to SLD |
| 5 | $\frac{1}{5-(4-1)}(151.2-30)=60.6$ | ----- | $90.6-60.6=30$ | Switch to SLD |

## Depreciation comparison

$\square$ DDBD and SLD is commonly used in Indonesia except SOYD
$\square$ DDBD is recommended if you want to find income after tax
$\square$ SOYD and DDBD are suitable for asset which the deterioration or loss the value is very quick
e.g: production machine

## Excel Function

=SLN(cost, salvage, life)
SOYD
=SYD(cost, salvage, life, period)
DDBD
=DDB(cost, salvage, life, period [factor])
DDBD conversion
=DDB(cost, salvage, life, start_period,End_period,[factor],
[no _switch])
Factor default 200\%/N

## After Tax Cash Flow

Taxable income $=\Sigma$ income- interest- Depreciation

Tax= taxable income $x$ tax rate (\%)

After Tax Cash Flow= Before Tax Cash Flow- tax

The more amount depreciation cost, the less taxable income and of course the tax as well

## Practice Problem

investment
Annual Benefit
Annual Cost
Over haul ${ }_{(t=5)}$
Salvage value
Useful life
Corporate tax

Rp 700 million
Rp 130 million
Rp 30 million
Rp 70 million
Rp 300 million
8 years
$10 \%$ per years
"how much will the corporate pay in income taxes for the year using SLD and DDBD?

## SLD Method

| n | Before tax cash flow |  |  | $\text { SLD }=1 / \mathrm{N}(I-$ <br> S) | Taxable income | $\begin{gathered} \operatorname{tax} \\ 10 \% \end{gathered}$ | After tax cash flow |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (-) | (+) | NCF |  |  |  |  |
| (a) | (b) | (c) | ( $\mathrm{d}=\mathrm{c}-\mathrm{b}$ ) | (e) | (f=d-e) | ( $\mathrm{g}=\mathrm{fx} 10 \%$ ) | ( $\mathrm{h}=\mathrm{d}-\mathrm{g}$ ) |
| 0 | 700 |  | -700 |  |  |  | -700 |
| 1 | 30 | 130 | 100 | 50 | 50 | 5 | 95 |
| 2 | 30 | 130 | 100 | 50 | 50 | 5 | 95 |
| 3 | 30 | 130 | 100 | 50 | 50 | 5 | 95 |
| 4 | 30 | 130 | 100 | 50 | 50 | 5 | 95 |
| 5 | 100 | 130 | 30 | 50 | -20 | 0 | 30 |
| 6 | 30 | 130 | 100 | 50 | 50 | 5 | 95 |
| 7 | 30 | 130 | 100 | 50 | 50 | 5 | 95 |
| 8 | 30 | 130 | 100 | 50 | 50 | 5 | 95 |
| S |  | 300 | 300 |  |  |  | 300 |

## DDBD Method

| n | Before tax cash flow |  |  | $\begin{gathered} \mathrm{DDBD}=2 / \mathrm{N} \\ \left(B V_{t}-1\right) \end{gathered}$ | $B V_{t}$ | Taxable income | Pajak 10 \% | After tax cash flow |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | (-) | (+) | NCF |  |  |  |  |  |
| (a) | (b) | (c) | ( $d=c-b$ ) | (e) | ( $\mathrm{ft}=\mathrm{dt}-1-\mathrm{BV}$ ) | ( $\mathrm{g}=\mathrm{d}-\mathrm{e}$ ) | ( $\mathrm{h}=\mathrm{gx} 10 \%$ ) | (i=d-h) |
| 0 | 700 |  | -700 |  | 700 |  |  | -700 |
| 1 | 30 | 130 | 100 | 175 | 525 | -75 | -7.5 | 107.5 |
| 2 | 30 | 130 | 100 | 131 | 393.75 | -31.25 | -3.125 | 103.125 |
| 3 | 30 | 130 | 100 | 98 | 295.31 | 1.5625 | 0.15625 | 99.84375 |
| 4 | 30 | 130 | 100 | 74 | 221.48 | 26.17188 | 2.6171875 | 97.38281 |
| 5 | 100 | 130 | 30 | 55 | 166.11 | -25.3711 | 0 | 30 |
| 6 | 30 | 130 | 100 | 42 | 124.58 | 58.47168 | 5.84716797 | 94.15283 |
| 7 | 30 | 130 | 100 | 31 | 93.44 | 68.85376 | 6.88537598 | 93.11462 |
| 8 | 30 | 130 | 100 | 23 | 70.08 | 76.64032 | 7.66403198 | 92.33597 |
| S |  | 300 | 300 |  |  |  |  | 300 |

